# The Influence of Molecular Shape upon Dielectric Relaxation Times. 

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#### Abstract

Measurements are recorded of the relaxation times $\tau$ at infinite dilution of 32 different solutes, including methyl, tert.-butyl, phenyl, diphenylyl, and naphthyl derivatives. Carbon tetrachloride is the solvent most frequently concerned. Correlations between $\tau$ and a number of properties of the solute are mentioned; the relationship of $\tau$ with mean polarisability multiplied by a " shape factor" is illustrated graphically.


As is well known, Debye's original formula (1) only very roughly forecasts the

$$
\begin{equation*}
\tau=4 \pi \eta r^{3} / k T \tag{1}
\end{equation*}
$$

relaxation time $\tau$ of a molecule from the radius $r$ and a coefficient of inner friction $\eta$. Practical attention has been given much more to the dependence of $\tau$ on $\eta$ than to $\tau$ on $r$ (cf. " Dielectrics," Trans. Faraday Soc., 1946, 42, A, for references and details). However, the model assumed for the derivation of (1), viz., a spherical polar molecule in a homogeneous uniform medium, is obviously too simple. Perrin ( J. Physique, 1934, 5, 497) considered an ellipsoid to be a better approximation to reality and replaced $r^{3}$ by products of appropriate half-axes; the idea has been further elaborated by Budo, Fischer, and Miyamoto (Physikal. Z., 1939, 40, 337). For another problem (cf. Barclay and Le Fèvre, J., 1950, 556; Holland and Le Fèvre, J., 1950, 2166; Angyal, Barclay, and Le Fèvre, J., 1950, 3370 ; Buckingham and Le Fèvre, J., 1952, 1932), the degrees by which molecules depart from spherical symmetry have been represented by "shape factors." It seemed possible that these might be introduced in an empirical amendment or alternative to (1). Accordingly, a preliminary survey has been made of the values of $\tau$ of about 30 different species, selected to have extensions along or across the directions of their resultant dipole moments.

## Experimental

Measurements have been made on solutions in carbon tetrachloride or benzene, the majority in the former. Power from an oscillator (incorporating a reflex Klystron, type CV-35), operating at 3109 Mc ., was fed to an $E_{010}$ cavity resonator. This was made from 4"-diameter brass rod, its depth being 4.5 cm . and internal radius 3.56 cm . It was fitted with a brass lid through the centre of which was a guide-hole (diameter 0.8 cm .). All surfaces were silverplated. Half-way down the wall were two diametrically opposed holes through which were inserted two silver-plated " magnetic" probes, each fixed in orientation by a counter-sunk screw adjustable from the top of the resonator when the lid (itself held by six screws) was removed. The energy from the oscillator to the resonator and that from the resonator to the detector was controlled by small rotations of the probe loops. The solution to be examined, in a silica tube, stood vertically through the guide-hole in the centre of the resonator lid. Power was taken from the resonator to a detector consisting of a silicon-tungsten rectifier (Sylvania Electric Co.) in series with a galvanometer. The frequency was progressively increased from below to above that for resonance, and the current-frequency curve recorded. As the width of this curve at
half-height, i.e., $\Delta f$, was $1-2$ Mc., a beat method was employed to obtain $\Delta f$ : power from the above oscillator was fed into a mixer with power from a similar oscillator adjusted to give a beat frequency within the range $13.5-18.5 \mathrm{Mc}$. The frequency of the main oscillator was adjusted to the two half-height frequencies in turn, and the beat frequencies were measured. Their difference gave $\Delta f$. Since the detector crystal on calibration had been found to follow the " square law," the $Q$ factor of the circuit was $f_{\text {resonance }} / \Delta f ; Q$ was determined successively for the pure solvent and for the solutions. The incremental loss tangent, $\Delta \tan \delta$, was $A\left(1 / Q_{2}-1 / Q_{1}\right)$, where suffix 1 refers to the solvent, 2 to the solute, 12 to the solution, and $A$ is a constant determined by the properties of the resonator.

The computation of $\tau$ has been based on the following argument, starting with Debye's equation (2) :

$$
\begin{equation*}
\Delta \tan \delta=\frac{\left(\varepsilon_{12}+2\right)^{2}}{\varepsilon_{12}} \cdot \frac{2 \pi f \tau}{\left(1+4 \pi^{2} f^{2} \tau^{2}\right)} \cdot \frac{4 \pi \mu^{2} \boldsymbol{N} c_{2}}{27 \boldsymbol{k} T} . \tag{2}
\end{equation*}
$$

in which $c_{2}$ is measured in moles of solute per c.c. and other symbols have their usual meanings. Since solutions have been made up by weight, concentrations are conveniently given as weight fractions of solute, $w_{2}$. Appropriate transformation of $c_{2}$ into $w_{2}$ allows (2) to be rewritten as (3):

$$
\begin{equation*}
\Delta \tan \delta=\left(\varepsilon_{12}+2\right)^{2} w_{2} d_{12} K / \varepsilon_{12} M_{2} \tag{3}
\end{equation*}
$$

where $K=8 \pi^{2} f \mu^{2} \boldsymbol{N} \tau / 27 \boldsymbol{k} T\left(1+4 \pi^{2} f^{2} \tau^{2}\right)$ and $M_{2}$ is the molecular weight of the solute. It is not necessary to know the dielectric constants and densities of the mixtures used. At the dilutions used in this work $\varepsilon_{12}$ and $d_{12}$ may be each taken as rectilinear with $w_{2}$. Insertion of $\varepsilon_{12}=$ $\varepsilon_{1}\left(1+\alpha w_{2}\right)$ and $d_{12}=d_{1}\left(1+\beta w_{2}\right)$ into (3), and differentiation with respect to $w_{2}$, etc., gives

$$
\begin{equation*}
\left[\mathrm{d}(\Delta \tan \delta) / \mathrm{d} w_{2}\right]_{w_{2}-0}=K d_{1}\left(\varepsilon_{1}+2\right)^{2} / M_{2} \varepsilon_{1} \tag{4}
\end{equation*}
$$

The left-hand side of (4) can be obtained from experiment (either by calculating the " line of best fit " of $\Delta \tan \delta$ against $w_{2}$, or as the mean $\left.\Sigma(\Delta \tan \delta) / \Sigma w_{2}\right)$; calling it $\psi$, we have ultimately (since $f$ is always ca. $3 \cdot 109 \times 10^{9}$ cycles $/ \mathrm{sec}$.) :

$$
\begin{equation*}
\tau=\frac{5 \cdot 1993 \times 10^{28} D \mu^{2}}{M_{2} T \psi} \pm\left[\frac{2 \cdot 7032 \times 10^{57} D^{2} \mu^{4}}{M_{2}^{2} T^{2} \psi^{2}}-2.6204 \times 10^{-21}\right]^{\frac{1}{2}} \tag{5}
\end{equation*}
$$

$D$ in (5) is $d_{1}\left(\varepsilon_{1}+2\right)^{2} / \varepsilon_{1}$; around room temperature it has the following values for the two solvents now used :

| $T,{ }^{\circ} \mathrm{K}$ | $\varepsilon$ | $d$ | D | $T,{ }^{\circ} \mathrm{K}$ | $\varepsilon$ | $d$ | D |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Carbon tetrachloride |  |  | Benzene |  |  |  |
| 295 | $2 \cdot 2323$ | 1.5900 | 12.758 | 295 | 9. 2784 | 0.8770 | $7 \cdot 046$ |
| 293 | $2 \cdot 2360$ | $1 \cdot 5940$ | 12.792 | 293 | $2 \cdot 2825$ | $0 \cdot 8791$ | $7 \cdot 0635$ |
| 291 | $2 \cdot 2398$ | 1-5979 | 12.824 | 291 | $2 \cdot 2866$ | 0.8812 | $7 \cdot 081$ |
| 289 | $2 \cdot 2435$ | 1•6019 | 12.857 | 289 | $2 \cdot 2905$ | $0 \cdot 8834$ | $7 \cdot 100$ |
| 288 | $2 \cdot 2454$ | $1 \cdot 6039$ | 12.874 | 288 | $2 \cdot 2925$ | $0 \cdot 8844$ | $7 \cdot 108$ |

The various solutes had the m. p.s or b. p.s recorded for pure specimens in Beilstein's "Handbuch." Methyl chloride and bromide were prepared and dissolved as indicated respectively by Barclay and Le Fèvre (loc. cit.) and Buckingham and Le Fèvre ( $J$., 1953, 3432).

Essential observations are recorded in Table 1; sub-headings give. in order, solute, solvent, and temperature. The variations in $Q$ for $w_{2}=0$ shown in Table 1 are due to the fact that the value of $Q$ of the resonator system seemed to be dependent upon the state of polish of the internal surfaces of the cavity : $Q$ was greatest immediately after silvering and decreased with age. Measurements were not taken chronologically in the order shown. However, the value of $\Delta \tan \delta$, derived from the differences of the values of $1 / Q$ for a given solution and its solvent, is independent of the actual magnitude of $1 / Q_{1}$, since $1 / Q_{12}$ and $1 / Q_{1}$ are equally affected.

Results, calculated by eqn. (5), are set out in Table 2. Experience, gained by repetitions and redeterminations at different dates, suggests that the smaller relaxation times $(\tau)$ may vary by about $\pm 15 \%$ and the larger (those over $10 \times 10^{-12} \mathrm{sec}$.) by $\pm 10 \%$; these ranges are indicated by the diameters of the circles surrounding the points on the Figure.

Three of these solute-solvent systems have been examined by other authors, who report values of $\tau$ not differing seriously from those now found (see Table 3).

Table 1. Dependence of incremental tan $\delta$ on concentration.

| $10^{5} w_{4}$ | $\Delta f$ (Mc.) | $10^{1} \mathrm{O}_{12}$ | $10^{3}(\Delta \tan \delta)$ | $10^{5}{ }^{\prime}$ | $\Delta f$ (Mc.) | $10^{4} / Q_{12}$ | $10^{3}(\Delta \tan \delta)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Methyl chloride, carbon tetrachloride, $20^{\circ}$ Nitrobenzene, benzcne, $20^{\circ}$ |  |  |  |  |  |  |  |
| 0 | $0 \cdot 71$ | $2 \cdot 28$ | - | 0 | 2.02 * | 6.50 * | - |
| 929 | $1 \cdot 17$ | $3 \cdot 76$ | 1.83 | 145 | 2.34* | $7 \cdot 53$ * | $1 \cdot 67$ |
| 971 | $1 \cdot 18$ | $3 \cdot 80$ | 1.87 | 290 | $2 \cdot 61$ * | 8.39 * | $3 \cdot 06$ |
| 1184 | 1.28 | $4 \cdot 12$ | $2 \cdot \underline{2}$ | 1344 | $5 \cdot 39$ * | 17.33* | 17.54 |
| Methyl bromide, carbon tetrachloride, $22^{\circ}$ |  |  |  | 0 292 | 1.10 2.11 | 3.54 6.79 | 4.03 |
| 0 | $1 \cdot 28$ | $4 \cdot 12$ | - | 553 | $2 \cdot 86$ | $6 \cdot 79$ $9 \cdot 20$ | 4.03 7.02 |
| 370 | $1 \cdot 34$ | $4 \cdot 31$ | $0 \cdot 236$ | 721 | 3-45 | 11-10 | $9 \cdot 37$ |
| 494 | $1 \cdot 36$ | $4 \cdot 37$ | $0 \cdot 310$ | o-Xylene, carbon tetrachloride, $14^{\circ}$ |  |  |  |
| 864 | $1 \cdot 52$ | $4 \cdot 89$ | 0.955 |  |  |  |  |
| 0 | $0 \cdot 94$ | $3 \cdot 02$ | - | 0 | $1 \cdot 13$ | $3 \cdot 63$ |  |
| 859 | $1 \cdot 11$ | 3-57 | $0 \cdot 682$ | 2465 | 1.39 | $4 \cdot 47$ | $1 \cdot 04$ |
| 0 | 0.91 | 2.93 | - | 8097 | $2 \cdot 01$ | $6 \cdot 47$ | 3.52 |
| 1866 | $1 \cdot 28$ | $4 \cdot 12$ | $1 \cdot 48$ | 8299 | 1.97 | 6.34 | $3 \cdot 36$ |


| Methyl icdide, carbon tetrachloride, |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | $29^{\circ}$ |  |  |
| 0 | 0.94 | 2.99 | - |
| 5970 | 1.82 | 5.85 | 3.55 |
| 8930 | 2.24 | 7.20 | 5.23 |
| Nitromethane, carbon | tetrachloride, | $22^{\circ}$ |  |
| 0 | 0.77 | 2.48 | - |
| 187 | 1.17 | 3.76 | 1.59 |
| 936 | 1.27 | 4.08 | 1.98 |


| Acetonitrile, carbon |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | tetrachloride, | $\mathbf{9} \mathbf{9}^{\circ}$ |  |
| 0 | $\mathbf{1 . 2 6}$ | $4 \cdot 05$ | - |
| 366 | 2.48 | 7.98 | $4 \cdot 87$ |
| 48.5 | $\mathbf{2 . 9 0}$ | 9.33 | 6.5 .5 |


| Toluene, carbon tetrachloride, $\mathbf{2 9}^{\circ}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | 0.82 | 2.64 | - |
| 2883 | 0.93 | 2.99 | 0.43 |
| 4774 | 1.00 | 3.22 | 0.72 |
| 7205 | 1.09 | 3.51 | 1.08 |

Fluorobenzene, carbon tetrachloride, $14^{\circ}$

| 0 | 1.16 | 3.73 | - |
| ---: | ---: | ---: | ---: |
| 1156 | 1.74 | 5.60 | 2.32 |
| 1458 | 1.90 | 6.11 | 2.95 |
| 1602 | 2.00 | 6.43 | 3.35 |
| 1729 | 2.09 | 6.72 | 3.71 |
| 1853 | 2.04 | 6.56 | 3.51 |

Chlorobenzene, carbon tetrachloride, $14^{\circ}$

| 0 | 1.23 | $3 \cdot 96$ | - |
| ---: | ---: | ---: | ---: |
| 379 | 1.54 | $4 \cdot 95$ | 1.23 |
| 737 | 1.78 | 5.73 | $2 \cdot 20$ |
| 1493 | $2 \cdot 51$ | 8.97 | $5 \cdot 10$ |

Bromobenzene, carbon tetrachloride, $\mathbf{2 4}^{\circ}$

| 0 | $1 \cdot 20$ | $3 \cdot 86$ | - |
| ---: | ---: | ---: | ---: |
| 2131 | $2 \cdot 70$ | $8 \cdot 68$ | $5 \cdot 98$ |
| 4.271 | 4.26 | $13 \cdot 70$ | $12 \cdot 20$ |


| Icdobenzene, carbon tetrachloride, |  |  |  |
| ---: | :---: | :---: | :---: |
| 0 | $14^{\circ}$ |  |  |
| 0 | 1.18 | 3.80 | - |
| 988 | 1.69 | 5.44 | 2.04 |
| 0 | 1.30 | $4 \cdot 18$ | - |
| 1497 | 2.22 | 7.14 | 3.67 |
| 1806 | 2.33 | 7.50 | 4.12 |


| Benzonitrile, carbon tetrachloride, $14^{\circ}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | $1 \cdot 19$ | $3 \cdot 83$ |  |
| 86 | $2 \cdot 10$ | 6.75 | $3 \cdot 62$ |
| 317 | $4 \cdot 86$ | 15.63 | $13 \cdot 96$ |
| 400 | $6 \cdot 14$ | $19 \cdot 75$ | 19.07 |
| 417 | 6.25 | $20 \cdot 10$ | 19.50 |
| 788 | $10 \cdot 09$ | $32 \cdot 45$ | 34.82 |
| 0 | $1 \cdot 36$ | $4 \cdot 37$ |  |
| 926 | $10 \cdot 50$ | 33.74 | 36.46 |


| m-Xylene, carbon tetrachloride, $14^{\circ}$ |  |  |  |
| :---: | :---: | :---: | :---: |
| 0 | $1 \cdot 29$ | 4-15 | - |
| 9839 | 1.56 | $5 \cdot 02$ | 1.08 |
| 9970 | 1.57 | 5.05 | $1 \cdot 12$ |
| 16,138 | 1.81 | 5.82 | $2 \cdot 07$ |
| 18,980 | 1.83 | $5 \cdot 89$ | $2 \cdot 16$ |
| 4-Chlorodiphenyl, benzene, $20^{\circ}$ |  |  |  |
| 0 | 1-16 | 3.73 | - |
| 666 | $1 \cdot 57$ | $5 \cdot 0.5$ | $1 \cdot 64$ |
| 1657 | $2 \cdot 25$ | $7 \cdot 24$ | $4 \cdot 35$ |
| 0 | $1 \cdot 14$ | $3 \cdot 67$ |  |
| 614 | 1.54 | 4.95 | $1 \cdot 59$ |
| 4-Nitrodiphenvl, benzene, $\mathbf{2 2}^{\circ}$ |  |  |  |
| 0 | 1.07 | 3.44 | - |
| 272 | $2 \cdot 32$ | $7 \cdot 47$ | 5.05 |
| 369 | $2 \cdot 89$ | $9 \cdot 30$ | $7 \cdot 26$ |
| 0 | $1 \cdot 02$ | $3 \cdot 28$ |  |
| 257 | $2 \cdot 29$ | $7 \cdot 37$ | $5 \cdot 07$ |
| 317 | $2 \cdot 59$ | 8.33 | $6 \cdot 26$ |

$\alpha$-Nitronaphthalene, carbon tetrachloride, $20^{\circ}$

| 0 | $1 \cdot 2 \cdot$ | $3 \cdot 92$ | - |
| ---: | :--- | :--- | :--- |
| 116 | $1 \cdot 95$ | $6 \cdot 27$ | $2 \cdot 91$ |
| 0 | $1 \cdot 25$ | $4 \cdot 62$ | -5 |
| 217 | 2.62 | 8.43 | $5 \cdot 47$ |

$\alpha$-Nitronaphthalene, benzente, $15^{\circ}$

| 0 | 1.22 | $3 \cdot 93$ |  |
| :---: | :---: | :---: | :---: |
| 68 | $1 \cdot 42_{5}$ | $4 \cdot 58$ | $0 \cdot 81$ |
| 22:) | 1.95 | $6 \cdot 27$ | 2.90 |
| 320 | $2 \cdot 24$ | 7.22 | $4 \cdot 08$ |

p-Chloronitrobenzene, carbon tetrachloride, $2 \mathfrak{j}^{\circ}$

| 0 | 1.23 | 3.96 | - |
| ---: | :---: | :---: | :---: |
| 418 | 2.72 | 8.75 | 5.94 |
| 433 | 2.74 | 8.81 | $\mathbf{6 . 0 2}$ |
|  | p-Nitrotoluene, | benzene, $22^{\circ}$ |  |
| 0 | 0.95 | 3.06 | - |
| 147 | 1.80 | 5.78 | $\mathbf{3 . 3 7}$ |
| 0 | 1.15 | 3.70 | - |
| 231 | 2.50 | 8.04 | 5.38 |

tert.-Butyl chloride, carbon tetrachloride, $24^{\circ}$

| 0 | 0.81 | $2 \cdot 61$ | - |
| ---: | ---: | ---: | ---: |
| 670 | 1.22 | 3.92 | $1 \cdot 64$ |
| 1020 | 1.50 | 4.83 | $2 \cdot 7.5$ |
| 1483 | 1.80 | $5 \cdot 79$ | 3.95 |
| 2067 | 2.12 | 6.82 | $5 \cdot 23$ |
| 2394 | 2.33 | 7.49 | 6.06 |

* The quartz tube in these observations was different from that used for all the others now reported.

Table 1. (Continued.)
$10^{5} w_{2} \quad \Delta f(\mathrm{Mc}.) \quad 10^{4} / Q_{12} \quad 10^{3}(\Delta \tan \delta) \quad 10^{5} w_{2} \quad \Delta f(\mathrm{Mc}.) \quad 10^{4} / Q_{12} \quad 10^{3}(\Delta \tan \delta)$
tert.-Butyl bromide, carbon tetrachloride, $20^{\circ}$

| 0 | 1.01 | 3.25 | - |
| ---: | ---: | ---: | ---: |
| 570 | 1.34 | 4.31 | 1.31 |
| 1957 | 2.12 | 6.82 | 4.43 |

tert.-Butyl iodide, carbon tetrachloride, $20^{\circ}$

| 0 | 0.78 | 2.51 | - |
| ---: | ---: | ---: | ---: |
| 567 | 1.07 | 3.44 | 1.16 |
| 1734 | 1.62 | 5.21 | 3.35 |
| 2048 | 1.90 | 6.11 | 4.47 |
| 2651 | 2.20 | 7.08 | 5.66 |

$\alpha$-Fluoronaphthalene, carbon tetrachloride, $14^{\circ}$

| 0 | 1.10 | 3.54 | - |
| ---: | ---: | ---: | ---: |
| 561 | 1.58 | 5.08 | 1.91 |
| 1728 | 1.93 | 6.21 | 3.31 |

$\beta$-Fluoronaphthalene, carbon tetrachloride, $15^{\circ}$

| 0 | 1.14 | 3.67 | - |
| ---: | ---: | ---: | ---: |
| 747 | 1.89 | 6.08 | $\mathbf{2 . 9 9}$ |
| 1413 | 2.54 | 8.17 | 5.58 |


| -Chloronaphthalene, carbon tetrachloride, $20^{\circ}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 1.10 | 3.54 | - |  |
| 271 | 1.33 | 4.28 | 0.92 |  |
| 1724 | 2.60 | 8.36 | 5.98 |  |
| 2005 | 2.79 | 8.97 | 6.73 |  |
| $\beta$-Chloronaphthalene, carbon tetrachloride, $12^{\circ}$ |  |  |  |  |
| 0 | 1.05 | 3.38 | - |  |
| 322 | 1.46 | 4.70 | 1.64 |  |
| 634 | 1.84 | 5.92 | 3.15 |  |

Table 2. Calculation of relaxation times.

| Solute | $\psi$ | Temp. | $M_{2}$ | $\mu, \mathrm{D}$ | $\begin{gathered} 10^{12} \tau \\ \text { sec. } \end{gathered}$ | Solute | $\psi$ | Temp. | $M_{2}$ | $\mu, \mathrm{D}$ | $\begin{gathered} 10^{12} \tau \\ \text { sec. } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{3} \mathrm{Cl}$ | $0 \cdot 192$ | $22^{\circ}$ | $50 \cdot 5$ | $1 \cdot 79$ | 1.8 | $1-\mathrm{C}_{10} \mathrm{H}_{7} \cdot \mathrm{NO}_{2}$ | $2 \cdot 52$ | $20^{\circ}$ | 173 | $3 \cdot 88$ | 19 |
| $\mathrm{CH}_{3} \mathrm{Br}$ | $0 \cdot 082$ | 20 | $94 \cdot 95$ | $1 \cdot 70$ | 1.8 |  | $1 \cdot 28$ | 15 | 173 | $3 \cdot 88$ | 17* |
| $\mathrm{CH}_{3} \mathrm{I}$ | 0.059 | 22 | 142 | 1.48 | $2 \cdot 5$ | $p-\mathrm{ClC}_{6} \mathrm{H}_{4} \cdot \mathrm{NO}$ | $1 \cdot 40$ | 20 | 157 | $2 \cdot 6$ | 25 |
| $\mathrm{CH}_{3} \cdot \mathrm{NO}_{2}$ | $0 \cdot 84$ | 22 | 61 | $3 \cdot 14$ | $3 \cdot 1$ | $p-\mathrm{CH}_{3} \cdot \mathrm{C}_{6} \mathrm{H}_{4} \cdot \mathrm{~N}$ | 22.31 | 22 | 137 | $4 \cdot 44$ | 19 * |
| $\mathrm{CH}_{3} \cdot \mathrm{CN}$ | 1.35 | 22 | 41 | $3 \cdot 38$ | 2.8 | $\mathrm{CMe}_{3} \mathrm{Cl}{ }^{\text {a }}$.... | . $0 \cdot 253$ | 24 | 92.5 | $2 \cdot 14$ | $3 \cdot 0$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{CH}_{3}$ | $0 \cdot 015$ | 22 | 92 | $0 \cdot 35$ | 6.7 | $\mathrm{CMe}_{3} \mathrm{Br}$ | $0 \cdot 226$ | 20 | 137 | $2 \cdot 19$ | $3 \cdot 75$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{~F}$ | $0 \cdot 203$ | 14 | 96.5 | $1 \cdot 44$ | $5 \cdot 4$ | $\mathrm{CMe}_{3} \mathrm{I}$ | $0 \cdot 214$ | 20 | 184 | $2 \cdot 14$ | $5 \cdot{ }^{5}$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$ | $0 \cdot 33$ | 14 | 112.6 | 1.58 | $8 \cdot 6$ | $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{~F}$ | $0 \cdot 30$ | 14 | 146 | $1 \cdot 35$ | 15 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ | $0 \cdot 285$ | 24 | 157 | 1.51 | 12 | $\beta$ - | $0 \cdot 40$ | 15 | 146 | 1.43 | 18 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{I}$ | $0 \cdot 23$ | 14 | 204 | 1.39 | 15 | $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{Cl}$ | $0 \cdot 34$ | 14 | 163 | $1 \cdot 42$ | 18 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{CN}$ | $4 \cdot 25$ | 14 | 103 | 4.02 | 17 | $\beta$ - | $0 \cdot 50$ | 12 | 163 | $1 \cdot 62$ | 20 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{NO}_{2}$ | 1.30 | 20 | 123 | 3.95 | 11* | $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{Br}$ | 0.31 | 12 | 207 | 1.41 | 21 |
| $o$-Xylene | $0 \cdot 041$ | 14 | 106 | $0 \cdot 53$ | $9 \cdot 0$ |  | $0 \cdot 37$ | 14 | 207 | 1.55 | 21 |
| $m$-Xylene | 0.012 | 14 | 106 | $0 \cdot 26$ | 11 | $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{I}$ | $0 \cdot 232$ | 12 | 254 | 1.32 | 23.5 |
| $4-\mathrm{C}_{6} \mathrm{H}_{4} \mathrm{Ph} \cdot \mathrm{Cl}$ | 0.26 | 20 | 189 | 1.56 | 32* |  | $0 \cdot 30$ | 12 | 254 | $1 \cdot 42$ | 27 |
| $4-\mathrm{C}_{6} \mathrm{H}_{4} \mathrm{Ph} \cdot \mathrm{NO}_{2}$ | 1.97 | 22 | 199 | $4 \cdot 17$ | 35* | Camphor | $0 \cdot 52$ | 15 | 152 | $2 \cdot 94$ | $9 \cdot 7$ |

Table 3. Previous determinations relevant to Table 2.

| Solute | Solvent | $10^{12} \tau$, sec. | Source |
| :---: | :---: | :---: | :---: |
| $\mathrm{CMe}_{3} \mathrm{Cl}$...... | $\mathrm{CCl}_{4}$ | $3 \cdot 4$ | Curtis, McGeer, Rathmann, and Smyth, J. Amer. Chem. Soc., 1952, 74, 644 |
| Camphor ...... | $\mathrm{C}_{6} \mathrm{H}_{6}$ | $9 \cdot 5$ | Whiffen, Trans. Faraday Soc., 1950, 46, 130 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{NO}_{2}$ | $\mathrm{C}_{6} \mathrm{H}_{6}$ | $12 \cdot 0$ | Spengler, Physikal. Z., 1941, 42, 134 |
| ," | ,' | 11.6 | Jackson and Powles, Trans. Faraday Soc., 1946, 42, A, 106 |
| " | , | 13.0 | Cripwell and Sutherland, ivid., p. 151 |
| " | , | 11.5 | Whiffen and Thomson, ibid., p. 118 |
| " | " | 12.8 12.7 | Whiffen, loc. cit. |
| " | " | 12.7 | Curtis et al., loc. cit. |

## Discussion

The results illustrate the general tendency for $\tau$ to increase with increasing molecular size or weight. Such behaviour has been noted before, particularly for certain homologous series (cf. Böttcher, "Theory of Dielectric Polarisation," Elsevier Publ. Co., 1952, Chap. 10, for references). Table 2, however, shows no smooth variation of $\tau$ with $M_{2}$. Since many of the solutes are solid at room temperature, the relation between $\tau$ and molar volume, taken as $M_{2} / d_{2}$, cannot be completely considered, although signs of a rough dependence may be seen for those compounds which are liquid. Various empirical and other properties of the substances listed have been plotted against $\tau$; e.g., the curve of parachor ( $P$ ) versus $\tau$ included all the values of $\tau$ within a rather wide "corridor." This was of interest since parachors provide relative measures of molecular volumes and can be computed with fair accuracy from known atom and bond "constants" (the figures in parentheses in Table 4 were estimated in this way from Vogel's Table XXII of $J ., 1948,1833$; the remainder are measurements given in Vogel's various papers). Neither the plot of the product $A B C$ (see later) nor that of the quctient $\mu^{2} / 3 \boldsymbol{k} T$ against $\tau$ was at all satisfactory; they were tried because they had the same order of magnitude (viz., $10^{-24}$ c.c.) as has $r^{3}$ in equation (1). A graph of $R_{2}$ against $\tau$ was suggestive : it contained all points in a band no

Table 4. Molecular dimensions, parachors, and refractivities.

|  | A | $B$ | C | $P$ | $R_{\text {D }}$ (c.c.) | $10^{24} \alpha_{\text {mean }}$ | $10^{3} h^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{CH}_{3} \mathrm{Cl}$................ | $5 \cdot 27$ | $3 \cdot 80$ | $3 \cdot 80$ | (111) | 11.5 | $4 \cdot 53$ | $26 \cdot 1$ |
| $\mathrm{CH}_{3} \mathrm{Br} \ldots . . . . . . . . . . . .$. | $5 \cdot 54$ | $3 \cdot 80$ | $3 \cdot 80$ | (124) | 14.5 | $5 \cdot 71$ | $35 \cdot 1$ |
| $\mathrm{CH}_{3} \mathrm{I}$. $\ldots \ldots \ldots \ldots \ldots .$. | $5 \cdot 92$ | $3 \cdot 80$ | $3 \cdot 80$ | (146) | 19.4 | $7 \cdot 64$ | $49 \cdot 2$ |
| $\mathrm{CH}_{3} \cdot \mathrm{NO}_{2} \ldots \ldots \ldots \ldots \ldots$ | $5 \cdot 20$ | $4 \cdot 50$ | $3 \cdot 80$ | 132 | $12 \cdot 5$ | $4 \cdot 93$ | $16 \cdot 1$ |
| $\mathrm{CH}_{3} \cdot \mathrm{CN}^{\text {a }} \ldots \ldots \ldots \ldots .$. | $5 \cdot 95$ | $3 \cdot 80$ | 3.80 | 122 | $11 \cdot 1$ | $4 \cdot 37$ | $50 \cdot 4$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{CH}_{3} \quad \ldots \ldots \ldots \ldots$. | $8 \cdot 25$ | 6.05 | $3 \cdot 80$ | 247 | $31 \cdot 1$ | 12.25 | $90 \cdot 7$ |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{~F}$. $\ldots \ldots \ldots \ldots \ldots .$. | 7.33 | 6.05 | $2 \cdot 90$ | 214 | $26 \cdot 0$ | $10 \cdot 2$ | 118 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Cl}$. $\ldots \ldots \ldots \ldots .$. | 8.08 | 6.05 | $3 \cdot 16$ | $244 \cdot 5$ | $31 \cdot 1$ | $12 \cdot 2{ }_{5}$ | 123 |
| $\mathrm{C}_{6} \mathrm{H}_{5}{ }^{5} \mathrm{Br} \quad \ldots \ldots \ldots \ldots .$. | $8 \cdot 20$ | 6.05 | $3 \cdot 40$ | 261 | $33 \cdot 9$ | 13.4 | 111 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{I}$. $\ldots \ldots \ldots \ldots \ldots \ldots .$. | 8.58 | 6.05 | $3 \cdot 64$ | 282 | $39 \cdot 1$ | $15 \cdot 4$ | 110 |
| $\mathrm{C}_{6} \mathrm{H}_{5}{ }^{\text {- }} \mathrm{CN} . . . . . . . . . . . .$. | $8 \cdot 95$ | 6.05 | 2.90 | 259 | 31.4 | $12 \cdot 4$ | 171.5 |
| $\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{NO}_{2}$ | $8 \cdot 00$ | 6.05 | $2 \cdot 90$ | $264 \cdot 5$ | $32 \cdot 7$ | $12 \cdot 9$ | 138 |
| o-Xylene .............. | 7.50 | 6.80 | $3 \cdot 80$ | 283 | $35 \cdot 8$ | $14 \cdot 1$ | $70 \cdot 75$ |
| $m$-Xylene $\ldots$......... | $6 \cdot 80$ | $8 \cdot 70$ | $3 \cdot 80$ | 284 | $35 \cdot 9$ | $14 \cdot 1$ | 98.3 |
| $4-\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{C}_{6} \mathrm{H}_{4} \cdot \mathrm{Cl} \ldots \ldots$. | $12 \cdot 40$ | 6.05 | $3 \cdot 16$ | (419) | $57 \cdot 8$ | $22 \cdot 8$ | 287 |
| $4-\mathrm{C}_{6} \mathrm{H}_{5} \cdot \mathrm{C}_{6} \mathrm{H}_{4} \cdot \mathrm{NO}_{2} \ldots$ | 12.32 | 6.05 | 2.90 | (435) | 56.4 | $22 \cdot 2$ | 305 |
| 1- $\mathrm{C}_{10} \mathrm{H}_{7} \cdot \mathrm{NO}_{2} \ldots \ldots . .$. | 8.00 | $8 \cdot 70$ | $2 \cdot 90$ | (369) | $50 \cdot 0_{6}$ | $19 \cdot 7$ | 156.5 |
| $p-\mathrm{Cl} \cdot \mathrm{C}_{6} \mathrm{H}_{4} \cdot \mathrm{NO}_{2} \ldots \ldots$. | $9 \cdot 41$ | 6.05 | $3 \cdot 16$ | (303) | 37.5 | $14 \cdot 8$ | 169 |
| $p-\mathrm{CH}_{3} \cdot \mathrm{C}_{6} \mathrm{H}_{4} \cdot \mathrm{NO}_{2}$ | $9 \cdot 57$ | 6.05 | $3 \cdot 80$ | 303 | $37 \cdot 4$ | 14.7 | 135 |
| $\mathrm{CMe}_{3} \mathrm{Cl}{ }^{\text {l }}$....... | 6.80 | 6.88 | $6 \cdot 88$ | (225) | $25 \cdot 8$ | $10 \cdot 2$ | $0 \cdot 0$ |
| $\mathrm{CMe}_{3} \mathrm{Br}$............. | 7.05 | 6.88 | 6.88 | (239) | 28.9 | 11.4 | $0 \cdot 1$ |
| $\mathrm{CMe}_{3} \mathrm{I}$................. | $7 \cdot 46$ | $6 \cdot 88$ | $6 \cdot 88$ | (260) | $34 \cdot 6$ | 13.6 | $1 \cdot 5$ |
| $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{~F} \ldots \ldots \ldots \ldots .$. | $7 \cdot 34$ | $8 \cdot 70$ | 2.90 | 321 | $43 \cdot 7$ | $17 \cdot 2$ | 154 |
| $\beta$ - | 9.79 | $7 \cdot 30$ | $2 \cdot 90$ | (321) | $43 \cdot 7$ | $17 \cdot 2$ | 183 |
| $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{Cl}$ | 8.00 | $8 \cdot 70$ | 3-16 | (350) | $49 \cdot 2$ | $19 \cdot 4$ | 138 |
| $\beta$ - | $10 \cdot 44$ | $7 \cdot 30$ | $3 \cdot 16$ | (350) | $49 \cdot 4$ | 19.5 | 183 |
| $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{Br}$ | $8 \cdot 28$ | $8 \cdot 70$ | $3 \cdot 40$ | (363) | $51 \cdot 6$ | $20 \cdot 3$ | 125 |
|  | 10.71 | $7 \cdot 30$ | $3 \cdot 40$ | (363) | $51 \cdot 8$ | $20 \cdot 4$ | 175 |
| $\alpha-\mathrm{C}_{10} \mathrm{H}_{7} \mathrm{I}$ | 8.60 | 8.70 | $3 \cdot 64$ | (386) | 56.5 | 22.3 22.8 | $114 \cdot 5$ |
| $B-$ ", | 11.02 | $7 \cdot 30$ | $3 \cdot 64$ | (386) | 57.9 | $22 \cdot 8$ | 169 |

wider than that of the parachor- $\tau$ plot, and placed related molecules (e.g., fluoro-, chloro-, bromo-, and iodo-benzenes) on individual straight lines having different inclinations to the $\tau$-axis.

When either parachors or refractivities were used, however, the three tert.-butyl halides stood on the lower fringe of the "corridor," as though their $\tau$ 's were abnormally low. Now, the small relaxation times of certain molecules of a near-spherical form have been noted by several workers (e.g., Smyth, Trans. Faraday Soc., 1946, 42, A, 175 ; Böttcher, op. cit., Chap. 10) ; it seemed, therefore, that multiplication of the parachors or refractivities by " shape factors" would improve the curves in question.

The dimensions given in Table 4 have been used as a basis. Their derivations from scale-drawings, etc., are explained in the papers by Le Fèvre and his colleagues cited on
p. 2873. Of various ratios and combinations of $A, B$, and $C$, that denoted as $h^{2}$ by Holland and Le Fèvre ( $J ., 1950,2166$ ) seemed to be most suitable (numerical values of $h^{2}$ are quoted in Table 4).


Empirical correlation of the velaxation times $(\tau)$ with shape factors and mean polarisabilities (see below), incorporating estimated experimental errors.

The figure depicts the best relationship, viz., $10^{12} \tau$ plotted against the product $10^{\mathbf{2 4}}$ $\left(\alpha_{\text {mean }}\right)\left(\exp h^{2}\right)^{2}$, so far extracted from the present data. (The average polarisability ( $\alpha_{\text {mean }}$ ) is directly calculable from the molecular refraction $R$.) The closeness of the points makes provision of a key difficult; $A, B$, and $C$, which are most out-of-line, refer respectively to $p$-chloronitrobenzene in carbon tetrachloride, $p$-nitrotoluene in benzene, and benzonitrile in carbon tetrachloride. In addition to experimental errors, and to the use of non-uniform temperatures, its imperfections must be, in part, due to neglect of solvent effects. The work of, inter al., Whiffen (Trans. Faraday Soc., 1950, 46, 130) indicates that a given medium will not influence the $\tau$ 's of all molecules alike (e.g., the relaxation times of nitrobenzene and camphor are slightly greater in carbon tetrachloride than in benzene; for chloroform the reverse is true). Hill (Nature, 1953, 171, 836) has plotted $\tau$ against the " mutual viscosities" for solute-solvent pairs made by six solutes and three solvents; an approximation to a straight line through the origin resulted. However, the Figure embraces a wider range of relaxation times and a greater number of solutes than were considered by Hill; further, it appears to do so more smoothly.

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